

www.jart.icat.unam.mx

Journal of Applied Research and Technology 21 (2023) 965-974

Original

Numerical and experimental performance analysis of a horizontal axis hydrokinetic turbine

J. D. Betancur Gómezª ● J. G. Ardila Marín^{b*} ● E. L. Chica Arrieta^c

a Instituto Tecnológico Metropolitano, Medellín, Colombia b Universidad Surcolombiana, Neiva, Colombia c Universidad de Antioquia, Medellín, Colombia

> Received 05 26 2022; accepted 01 12 2023 Available 12 31 2023

Abstract: Alternative technologies such as hydrokinetic turbines can improve electric energy conditions in rural or non-interconnected areas with a low environmental impact. However, as they are an emergent device, they must be studied further to better understand their phenomenology and the ways to improve their performance. The numerical and experimental evaluation of rotors under specific operation conditions, depending on their hydrodynamic profiles, result in efficiency curves for evaluated prototypes, so that devices are proposed which take full advantage of the flow conditions of a specific place. Considering the above, the main objective of this work was to evaluate a horizontal-axis hydrokinetic turbine rotor prototype numerically and experimentally with an EPPLER E817 hydrodynamic profile for a flow velocity of 1,4 m s-1. The simulations were conducted by means of computational fluid dynamics; the k-ω SST turbulence model was used, and the torque was monitored. Then, the grid convergence index (GCI) was calculated to establish the results' numerical uncertainty. For experimentation, the rotor was additively manufactured and evaluated in a test bench, where tests at velocity of 1.4 m s^{-1} were performed and the braking voltage was varied to measure torque at different tip speed ratio (TSR). Finally, the experimental and numerical curves of power coefficient (Cp) versus TSR were compared. Both the simulation and experimental results show that a TSR of about 4 represents the best operating conditions, but, due to mechanical losses in the experimental setup, the reported Cp values differ between a numerical 0,434 and an experimental 0,267. The power generated by the evaluated rotor could achieve 117,0 W, thus showing the potential of this technology for electrical power supply with low environmental impact.

Keywords: Turbomachine, hydrofoil, computational fluid dynamics, numerical uncertainty

1. Introduction

Environmental and energy problems worldwide have forced researchers to seek sustainable energy solutions. They have found renewable alternatives such as wind, sun, and water to generate clean and environmentally friendly energy [\(Djørup et](#page-6-0) [al., 2018; Erdiwansyah et al., 2019; Hansen et al., 2019; Nicolli](#page-6-0) [& Vona, 2019\)](#page-6-0). The energy available from water resources is the world's largest and cheapest [\(Yuce & Muratoglu, 2015\)](#page-6-0). Large hydroelectric dams have been criticized because they require large dams and infrastructure that cause damage to the environment and ecosystems [\(Hoq et al., 2011\)](#page-6-0). Accordingly, small hydroelectric plants have become one of the most economical and environmentally friendly sources of energy generation in rural areas [\(Woodruff, 2007\)](#page-6-0). There are two techniques to extract energy from water: hydrostatic and hydrokinetic. Hydrostatic techniques use turbomachinery to extract the potential energy from the pressure head [\(Khan et](#page-6-0) [al., 2008\)](#page-6-0). Hydrokinetic techniques (HKTs) use the kinetic energy of channels, tides, oceans, and rivers along with turbo machinery to generate energy. Diverse numerical and experimental research has been conducted worldwide regarding HKTs, with the purpose of improving the performance of different rotors [\(Goundar & Ahmed, 2013;](#page-6-0) [Wang et al., 2019\)](#page-6-0)[. Table 1](#page-1-0) summarizes the most recent results.

Computational fluid dynamics (CFD) software is widely used to simulate the behavior of fluids such as water and air, given that they represent an economical way of obtaining results close to reality. For this reason, many authors have used CFD software to solve physical phenomena ([Betancur et](#page-6-0) [al., 2019; Esfahanian et al., 2013;](#page-6-0) Sufian et al., 2017)[. Tian et al.](#page-6-0) [\(2018\)](#page-6-0) performed three-dimensional simulations of a hydrokinetic turbine with three blades. They used the shear stress transport k-ω SST turbulence model. The numerical results were compared to experimental ones. In a study b[y Lee](#page-6-0) [et al. \(2012\),](#page-6-0) a three-dimensional simulation with the blades of a hydrokinetic turbine was conducted. As a result, power coefficient vs. TSR curves were obtained and compared with experimental and other numerical results. [Pujol et al. \(2015\)](#page-6-0) conducted a study on the geometry of the water wheel to improve its efficiency. The results of the simulation were reported with uncertainty using the grid convergence index (GCI), and they were finally compared to experimental results.

Few articles have reported the numerical uncertainty of three-dimensional simulations; it is a complex task due to the sensitivity of the performance variables and the high computational cost. One of the techniques used to determine numerical uncertainty by means of systematic refinement is the GCI ([Karaalioglu & Bal, 2022; Liu et al., 2022; Mohamed et](#page-6-0) [al., 2020; Paudel & Saenger, 2017; Pujol et al., 2015; Roy &](#page-6-0) [Blottner, 2006](#page-6-0)). GCI is based on Richardson's extrapolation theory, which is used for discrete solutions with different grid densities [\(Roache, 1998\)](#page-6-0). In this work, we managed to quantify the numerical uncertainty of a three-dimensional CFD simulation for a horizontal-axis hydrokinetic turbine. Three grids with different element densities were used to calculate the uncertainty of the numerical results. Torque (τ) was the output variable used to quantify numerical uncertainty.

Table 1. Recent state of the art.

Thereupon, this article is structured as follows. The first section shows the way in which the CFD simulation was configured. Then, the calculation of the numerical uncertainty is presented. Next, the physical model and the experiment are described. In the following section, the results of the simulation are presented, where the obtained behavior of the fluid near the turbine is compared with other similar studies. Moreover, the GCI results and the performance graph of the turbine, along with its corresponding numerical uncertainty, are presented. Then, the experimental and numerical results are compared. Finally, a discussion about the results is proposed, and the conclusions are presented.

2. Materials and methods

2.1. CFD simulation

For the three-dimensional simulation, the CFX® module of ANSYS® was used. To elaborate the grid, an HP Workstation Z600 with a 2,66 GHz processor, 48 GB of RAM, and 12 processing cores was used. For the simulations, a DELL T7600 Workstation with a 2,9 GHz processor and 32 GB of RAM was employed, as well as 12 cores in parallel for a double precision solution. For this study, the geometry of a rotor was imported, which was built with the EPPLER 817 hydrofoil in previous research ([Betancur et al., 2020\)](#page-6-0) through BEM (Blade Element Methodology) modeling. Moreover, the k-w SST turbulence model was used, given its wide use in research regarding hydrokinetic turbine applications, as well as the accuracy it offers due to the treatment near the geometry walls, where the grid was densified to ensure the y+ recommended for the model of 0,02 [\(Tian et al., 2018\)](#page-6-0).

Once the solid model of the turbine was imported, Boolean operations were performed to create two different fluids. The first is a rotating fluid that contains the rotor and is built from a circle with a 1 D radius [\(Jeffcoate et al., 2016\)](#page-6-0) and a height of 1 ⅓ D, where D is a rotor diameter equal a 0,5 m. The second is a stationary fluid containing the first, which enters freely and contrary to the axis. This control volume has a total length of 5 ½ D and a radius of 2 ½ D [\(Kim et al., 2017\)](#page-6-0). I[n Figure 1,](#page-2-0) the two control volumes and the turbine rotor can be observed. Since it is a symmetrical geometry that repeats itself three times, a third of the total volume is simulated to save computation times. This simplification does not affect the results according to [\(Lee et al., 2012; Yang et al., 2014\)](#page-6-0). The design methodology in the discussion on details regarding the solver configuration can be consulted in previous research ([Betancur et al., 2020](#page-6-0)), the rotor has a diameter of 0,5 m, 3 equidistant blades, with a maximum chord of 0,0957 m and a minimum of 0,0404 m, and a warpage of 42,3° at the base and 5,85° at the tip.

A grid was built in the control volumes of the exterior fluid and the one surrounding the rotor. The grid was elaborated on the Meshing® module of ANSYS®. An inflation with five layers

around the blade was used, as shown in [Figure 2a.](#page-2-1) This area was densified (see [Figure 2b\)](#page-2-1) since it is where the phenomenology of interest takes place. The mesh of this fluid [\(Figure 2c\)](#page-2-1) is composed of hexahedra surrounding the blade and tetrahedra in the rest of the volume. Then, the minimum element measurement was parameterized to densify the mesh in a structured way and generate other two. [Table 2](#page-2-2) presents the details and the main metrics of the three meshes created. The accepted range for orthogonal quality is 0,15-1. The acceptability range for the maximum skewness is between 0 and 0,94, and the aspect ratio must be lower than 30 ([ANSYS,](#page-6-0) [2010\)](#page-6-0). As can be observed, all metrics of each mesh comply with the acceptability ranges.

Figure 1. Control volume with the rotor.

Figure 2. a) Inflation around the blade, b) element density in the blade, c) rotational control volume.

Table 2. Mesh details and metrics.

[Figure 3](#page-3-0) shows the borders defining the regions of the fluids to be simulated and the boundary conditions of the control volume. Symmetry interfaces were defined in the flat faces of the control volume to indicate that the phenomenology is repeated in the next section. The values with which each of the

regions were configured are reported in [Table 3,](#page-3-1) namely normal velocity on entry, relative pressure on exit of 0 Pa, noslip condition on the wall rotor, and periodic rotational condition in the symmetry interfaces established between the two fluid volumes defined above.

Figure 3. Border conditions of the system.

A transitory 4s simulation was configured with an adaptive time-stepping varying between 0,01 s and 0,00001 s. This time stepping was established using the Courant number equation, for which the smallest mesh element size was used, as well as the lowest fluid velocity on the blade's surface, which is the point where these mesh elements appear. The outer domain is considered stationary, and the fluid surrounding the rotor is configured to rotate between 1 to 385 rpm. The frameshift was configured as "Frozen rotor," and the interface model was of general connection, whereas, for the periodical interfaces, the interface model was periodical-rotational. When the configuration was done, the torque on the blade surface was selected as the monitoring variable. Furthermore, a highresolution was used for the advection scheme, the secondorder Backward Euler equation, a 1E-4 convergence criterion, and double precision.

2.2. Quantification of numerical uncertain

Given the increase in research on CFD, studies have been conducted which aim to improve the quality of the results. For this reason, some authors have proposed new practices that contemplate numerical uncertainty, which had not been considered thus far [\(Celik, 1993\)](#page-6-0). Numerical uncertainty is due to the errors involved in the numerical modeling of the Navier-Stokes equations and includes the influence of discretization errors, rounding error, and iterative convergence [\(Eça & Hoekstra,](#page-6-0) [2009; Freitas, 2002; Roy, 2005\)](#page-6-0). Moreover, it cannot be eliminated, but it must be minimized and quantified [\(Freitas, 2002\)](#page-6-0), so it is recommended to use the GCI to calculate it and therefore determine a simulation's level of accuracy [\(Freitas, 2002\)](#page-6-0).

To calculate the GCI, the representative cell or grid size *h* is first defined. Three-dimensional calculations are performed with the Equation (1).

$$
h = \left[\frac{1}{N}\sum_{i=1}^{N} (\Delta V_i)\right]^{\frac{1}{3}}
$$
\n⁽¹⁾

Where ΔV_i is the volume of cell *i*, and *N* is the total number of cells used.

Then, three grids must be selected: a fine one (*m1*), a medium one (*m2*), and a course one (*m3*). Once the key or significant variable (*φ)* is obtained, the refinement factor (*r)* is calculated, so that $r = h_{coarse}/h_{fine}$ is greater than 1,3. Grid refinement must be systematic and structured. The monitored variable (φ) in this study was torque. Once $h_1 < h_2 < h_3$ and $r_{21} = h_2/h_1, r_{32} = h_3/h_2$, the apparent order of convergence (*p)* is calculated using the Equation (2).

$$
p = \frac{1}{\ln(r_{21})} |\ln|\varepsilon_{32}/\varepsilon_{21}| + q(p)| \tag{2}
$$

Where $\varepsilon_{32} = \varphi_3 - \varphi_2$, $\varepsilon_{21} = \varphi_2 - \varphi_1$, and φ_k , where *k* is the grid level*.* For the asymptotic solution of *p, q(p)* should approximate 0 for a constant *r* (Equation (3)).

$$
q(p) = \ln \left(\frac{r_{21}^p - s}{r_{32}^p - s} \right) \tag{3}
$$

The convergence condition (R) is evaluated with the Equation (4).

$$
R = \frac{\varphi_1 - \varphi_2}{\varphi_2 - \varphi_3} \tag{4}
$$

The possible results of Equation (4) are: If $0 < R < 1$, monotonous convergence. If R < 0, oscillatory convergence. If *R* > 1, divergence.

[Roache \(1994\)](#page-6-0) combines the concept of safety factor with absolute values to generate the error bar instead of the estimation of the error. As a result, the numerical uncertainty is obtained, which is also known as the grid convergence index (GCI) and is calculated with the Equation (5).

$$
GCI = \frac{F_S}{r_{21}^p - 1} \left| \frac{\varphi_2 - \varphi_1}{\varphi_1} \right| \tag{5}
$$

Where F_s is the safety factor. For three grids, Roache recommends using a safety factor of 1,25 [\(Roache, 1994; 1998\)](#page-6-0). This index may be understood as an estimation of the error

associated with solving the grid, and it indicates how much the solution will change with a more refined grid.

2.3. Experimental setup

The physical model consists of a system comprising a mobile support, a casing, a turbine, and an instrument box that are attached to a trolley type cart that moves guided within a fixed rail, as seen i[n Figure 4.](#page-4-0)

Figure 4. Test bench.

This system can be moved at different velocities since it has a frequency driver that controls a 1 HP motor, which has a pulley on its axis with a steel wire. One end of the wire is fixed to the mobile support, which allows it to move along a 21 m rail located at the edge of a semi-Olympic swimming pool. The casing and turbine systems are submerged at a depth of 0,8 m, 1 m from the wall, and 0,7 m from the bottom. The rotor used for this experiment is the same as that was used in the simulation, but at a scale of 1:2. Inside the bearing, there is a sensor that allows measuring the torque and the angular velocity in the turbine. It has a motor that serves as a brake and flexible coupling to complete the installation. The rotary torque sensor is a FUTEK® of up to 50 Nm. It provides measurements with a precision of 0,2%, and it has a 0,1% hysteresis and a 0,2% unrepeatability, as well as a certified factory calibration under the ISO 17025 norm.

As an input variable, the flow velocity of the test stand was evaluated with a velocity of around 1,4 m s⁻¹. The velocity at which the system moves has the same magnitude as the velocity of the water(U_{∞}), but in the opposite direction. The latter is measured indirectly by means of the distance and time. The distance is given by a series of sensors located 4,0 m away from each other along the rail, where the time between one and the other is measured by an Arduino® board. For each test, three-time values were obtained. The data were processed in a

spreadsheet to find the average value and the uncertainty. Then, they were related to obtaining the combined velocity and the uncertainty. After testing at different frequencies, it was found that, with a 0,6Hz frequency in the driver, the test stand moved at a velocity of approximately 1.4 m s^{-1} .

The revolutions per minute were monitored with the DC motor's voltage, which was varied from 0 to 3,8 V to achieve constant rotational speeds. The system was stabilized three seconds after startup, and during the following nine seconds, the first and second output variables were obtained, namely the turbine's revolutions per minute and the torque.

To elaborate the rotor's operation curve, it needs to be evaluated for TSR between 1 and 6 while varying the voltage. The values of the second output variable were multiplied by the rotation speed in RPM. This term, divided by the hydraulic power, results in the rotor's power coefficient or performance. With these data, the characteristic curve of Cp vs. TSR is elaborated for each rotor.

Noise factors or error causes were also identified, such as weather or environmental conditions at the testing site, namely stirring or resting states in the pool's water, deformation and/or vibrations suffered by the test stand, rotor roughness, braking in the bearings supporting the turbine axis, and others.

The data obtained with the sensor were exported to a spreadsheet, and, for each observation, the following procedure was conducted: the RPM data were filtered, and between 50 and 100 values were obtained for each value; the RPM were associated with a TSR by means of Equation (6); the average of the torque values associated with this TSR was found; and the standard deviation was calculated with Equation (7).

$$
TSR = \frac{\pi R P M r}{30 U_{\infty}} \tag{6}
$$

Where U_{∞} is fluid velocity, and r is the radius of the rotor.

$$
\sigma = \sqrt{\frac{1}{n-1} \sum (x_i - x)^2} \tag{7}
$$

Where x_i is each measured value, n is the amount of data, and x is the average value. To report the deviation of averaged data, the standard deviation of the mean must be calculated with Equation (8).

$$
\sigma_m = \frac{\sigma}{\sqrt{n}}\tag{8}
$$

The torque values (T) and RPM are taken to Equation (9) to calculate the power coefficient.

$$
C_p = \frac{T(RPM)}{15\rho U_{\infty}^3 r^2} \tag{9}
$$

Where ρ is the water density at ambient temperature. To calculate the combined uncertainty of C_n , Equation (10) is used.

$$
\delta C_p = \left[\sqrt{\left(\frac{\delta \boldsymbol{T}}{|\boldsymbol{T}|}\right)^2 + \left(\frac{\delta \boldsymbol{R} \boldsymbol{P} \boldsymbol{M}}{|\boldsymbol{R} \boldsymbol{P} \boldsymbol{M}|}\right)^2 + \left(\frac{\delta \boldsymbol{U_{\infty}}}{|\boldsymbol{U_{\infty}}|}\right)^2 + \left(\frac{\delta \boldsymbol{r}}{|\boldsymbol{r}|}\right)^2} \right] \big| \boldsymbol{C_p} \big| \quad (10)
$$

Where δT is the torque uncertainty, δRPM is the RPM uncertainty, and δU_{∞} is the fluid velocity uncertainty.

3. Results and discussion

[Figure 5](#page-5-0) shows a curve corresponding to the behavior of the observation variable (torque) in a transitory 4s simulation for the finest mesh. It can be evidenced that, initially, the torque shows an irregular behavior, where it reaches its maximum and minimum points. After the first second, the torque starts to stabilize and manages to remain constant from second 3 until the end. The same behavior was evidenced for grids 1 and 2.

Figure 5. Behavior of the output variable in terms of time for the finest grid.

[Figure 6](#page-5-1) shows three points that represent the torque behavior as the mesh densifies. The first point at the beginning of the graph for 7,94E5 elements with a torque of 3,23084 Nm. The second point is with 1,65E6 elements and a torque of 3,18678 Nm and the last point with the finest mesh of 1,03E7 elements and a torque of 3,15496 Nm. As the number of elements increases, the torque decreases. This is because the finer meshes contain more elements, therefore they capture the studied phenomenon with greater precision.

GCI is calculated using torque as the main variable. As the value of R is 0,722, and it is between 0 and 1, it is said that the convergence condition for the torque is monotonous. Furthermore, the GCI was calculated for grid 1 (GCI₁₂) and 2 (GCI₂₃) with a safety factor of 1,25, thus obtaining values of 0,203 and 1,449, respectively. The results show that, as the grid becomes denser, the error decreases. For this razon the finest grid was chosen to continue with the second part of the investigation.

For this study, the TSR was varied only between 0,1 and 6, to obtain torque values at different TSR, and the power coefficient was calculated by means of Equation (6). In [Figure](#page-5-2) 7, the performance curve of the simulated rotor is shown, as well as the numerical uncertainty calculated with the GCI. It can be evidenced that, as the TSR increases, the power coefficient does as well, up to TSR=4, where it starts to decrease. On the other hand, the error bar varies proportionately to the power coefficient. [Figure 7](#page-5-2) shows the curves of the power coefficient versus TSR elaborated from the experimental and numerical results. The behavior of the experimental and simulation curves is similar; the Cp values increase as the TSR increases, and, when a TSR between 3 and 4 is achieved, the Cp reaches its maximum point and starts to decrease. For TSR higher than 4,5, high RPM are required, and given the distance limitations of the test stand, these speeds could not be achieved. Therefore, the results obtained in the experimental curves only get to that point. The experimental uncertainty calculated with Equation (10) was 0,0057 the lowest for TSR 1,67 and 0,054 the highest for TSR 3,86.

Figure 6. Torque behavior for grid convergence index (GCI).

Figure 7. Experimental and numerical curve of the rotor designed with the EPPLER profile.

Experimental and numerical maximum Cp difference was 38,48%. The difference between the numerical and experimental results is due to several factors. The first of them is the mechanical loss occurring in the hermetic casing given

the packing used to provide the axis inlet with tightness. Although the couplings are high efficiency, there are critical areas such as the seal, where there may be losses due to friction with the axis. Another factor that causes the difference between the numerical and experimental results to be high is the control over the test stand's speed. The average velocity data for the test stand was 1.36 m $s⁻¹$, with a standard mean deviation of 0,06. This value is because the rails on which the cart moves are irregular, which causes mild braking in some segments, slight jamming, and other types of phenomena which are difficult to control. The fluid velocity increase and decrease considerably affect the power coefficient value [\(Lin et al., 2017\)](#page-6-0).

The greatest contribution of this work is the experimental validation of numerical results. As can be seen in [Table 1,](#page-1-0) few studies conduct this validation. Numerical studies simulate turbines between 1 and 10 m. Only [Sandoval et al. \(2021\)](#page-6-0) and [Lazzerini et al. \(2022\)](#page-6-0) numerically study turbines smaller than 0,27 and 0,42 m, respectively. While the experimental studies evaluate turbines on a scale between 0,109 and 0,8 m. Only [Lazzerini et al. \(2022\)](#page-6-0) simulated the rotor to be the same size as the scale model they experimented with. They used a hydrofoil like the one in the presented study and obtained a Cp consistent with the results reported here. [Table 1](#page-1-0) shows that the Eppler hydrofoil family is of great research interest and that the Cp found varies between 0,27 and 0,42. This is supported by the results of this work, whose experimental finding coincides with [Abutunis et al. \(2020\),](#page-6-0) while the numerical one agrees wit[h Aguilar et al. \(2021\).](#page-6-0) Finally, it is highlighted that the numerical Cp between 0,33 and 0,51 are higher than the experimental ones between 0,27 and 0,45, this study being conclusive as to the cause of the difference.

4. Conclusions

A horizontal-axis hydrokinetic turbine rotor designed with the EPPLER E817 hydro profile was numerically and experimentally evaluated. The power generated according to the maximum power coefficient is 117,0 W.

The GCI is an especially useful technique that allows obtaining reliable results with a lower number of grids to achieve independence. Therefore, it saves time and computational space. Furthermore, it allows obtaining the error bars at each point, which indicates the reliability of the results. But the immediate selection of the mesh sizes that will yield independence requires a lot of experience, so it is possible that in preliminary explorations it will be necessary to simulate many meshes, as many as in conventional independence studies, until finding those element sizes that will guarantee an appropriate asymptotic result value by Richardson extrapolation.

Even though the difference between the numerical and experimental results is large, the behavior of both curves is similar, and the error between them may be attributed to mechanical losses, as was previously mentioned.

For future works, the corrections will be applied to the bench to reduce the error associated with mechanical losses. The simulation will also be calibrated so that it considers some factors that it currently does not consider and that are unavoidable in the experiment.

Conflict of interest

The authors confirm that there is no conflict of interest to declare for this publication.

Acknowledgments

Thanks to Instituto Tecnológico Metropolitano for providing the human talent and economic resources from P17209 project and to Universidad de Antioquia and Universidad Surcolombiana for providing the human talent of their researchers to conduct this project.

Funding

This work was supported by the Instituto Tecnológico Metropolitano through an internal call for research projects [Project P17209, 2018]; The translation of this article was supported by the Universidad Surcolombiana through a contracting process advanced by the Vice-Rector for Research and Social Projection [Contract OC 062, 2021].

References

Abutunis, A., Taylor, G., Fal, M., & Chandrashekhara, K. (2020). Experimental evaluation of coaxial horizontal axis hydrokinetic composite turbine system. *Renewable Energy*, *157*, 232-245. <https://doi.org/10.1016/j.renene.2020.05.010>

Aguilar, J., Velásquez, L., Romero, F., Betancour, J., Rubio-Clemente, A., & Chica, E. (2021). Numerical and experimental study of hydrofoil-flap arrangements for hydrokinetic turbine applications. *Journal of King Saud University-Engineering Sciences*. <https://doi.org/10.1016/j.jksues.2021.08.002>

Alipour, R., Alipour, R., Fardian, F., & Tahan, M. H. (2022). Optimum performance of a horizontal axis tidal current turbine: A numerical parametric study and experimental validation. *Energy Conversion and Management*, *258*, 115533. <https://doi.org/10.1016/j.enconman.2022.115533>

ANSYS (2010)[. ANSYS 13.0 Meshing User'](https://www.researchgate.net/profile/Mohamed-Mourad-Lafifi/post/How_to_remove_warpage_angle_and_violation_of_heuristic_criterion_warning_in_LS-Dyna/attachment/5d0c0713cfe4a7968dacddf1/AS%3A771994878496770%401561069330997/download/Meshing_Tutorial_Ans.sys.pdf)s Guide. pp. 106–115.

Betancur, G, J. D., Ardila M, J. G., Ruiz S, A., & Chica A, E. L. (2019). [Aerodynamic profiles for applications in horizontal axis](https://papers.ssrn.com/sol3/papers.cfm?abstract_id=3453640) hydrokinetic turbines. [International Journal of Mechanical](https://papers.ssrn.com/sol3/papers.cfm?abstract_id=3453640) [Engineering and Technology,](https://papers.ssrn.com/sol3/papers.cfm?abstract_id=3453640) 10(3).

Betancur, J. D., Marin, J. G. A., & Arrieta, E. L. C. (2020). Design and hydrodynamic analysis of horizontal-axis hydrokinetic turbines with three different hydrofoils by CFD. *Journal of Applied Engineering Science*, *18*(4), 529-536. <https://doi.org/10.5937/jaes0-25273>

Celik, I. (1993). Numerical uncertainty in fluid flow calculations: needs for future research. <https://doi.org/10.1115/1.2910123>

Djørup, S., Thellufsen, J. Z., & Sorknæs, P. (2018). The electricity market in a renewable energy system. *Energy*, *162*, 148-157. <https://doi.org/10.1016/j.energy.2018.07.100>

Eça, L., & Hoekstra, M. (2009). Evaluation of numerical error estimation based on grid refinement studies with the method of the manufactured solutions. *Computers & Fluids*, *38*(8), 1580-1591. <https://doi.org/10.1016/j.compfluid.2009.01.003>

Erdiwansyah., Mamat, R., Sani, M. S. M., & Sudhakar, K. (2019). Renewable energy in Southeast Asia: Policies and recommendations.*Science of the total environment*, *670*, 1095-1102. <https://doi.org/10.1016/j.scitotenv.2019.03.273>

Esfahanian, V., Pour, A. S., Harsini, I., Haghani, A., Pasandeh, R., Shahbazi, A., & Ahmadi, G. (2013). Numerical analysis of flow field around NREL Phase II wind turbine by a hybrid CFD/BEM method. *Journal of Wind Engineering and Industrial Aerodynamics*, *120*, 29-36.

<https://doi.org/10.1016/j.jweia.2013.06.006>

Fontaine, A. A., Straka, W. A., Meyer, R. S., Jonson, M. L., Young, S. D., & Neary, V. S. (2020). Performance and wake flow characterization of a 1: 8.7-scale reference USDOE MHKF1 hydrokinetic turbine to establish a verification and validation test database. *Renewable Energy*, *159*, 451-467. <https://doi.org/10.1016/j.renene.2020.05.166>

Freitas, C. J. (2002). The issue of numerical uncertainty. *Applied Mathematical Modelling*, *26*(2), 237-248. [https://doi.org/10.1016/S0307](https://doi.org/10.1016/S0307-904X(01)00058-0)-904X(01)00058-0

Gish, L. A., Carandang, A., & Hawbaker, G. (2020). Experimental evaluation of a shrouded horizontal axis hydrokinetic turbine with pre-swirl stators. *Ocean Engineering*, *204*, 107252. <https://doi.org/10.1016/j.oceaneng.2020.107252>

Goundar, J. N., & Ahmed, M. R. (2013). Design of a horizontal axis tidal current turbine. *Applied energy*, *111*, 161-174. <https://doi.org/10.1016/j.apenergy.2013.04.064>

Gupta, M. K., & Subbarao, P. M. V. (2020). Development of a semi-analytical model to select a suitable airfoil section for blades of horizontal axis hydrokinetic turbine. *Energy Reports*, *6*, 32-37.

<https://doi.org/10.1016/j.egyr.2019.08.014>

Hansen, K., Breyer, C., & Lund, H. (2019). Status and perspectives on 100% renewable energy systems. *Energy*, *175*, 471-480. <https://doi.org/10.1016/j.energy.2019.03.092>

Hazim, S., El Ouatouati, A., Janan, M. T., & Ghennioui, A. (2020). Performance of a hydrokinetic turbine using a theoretical approach. *Energy Reports*, *6*, 317-324. <https://doi.org/10.1016/j.egyr.2019.08.062>

Hoq, T., Nawshad, U. A., Islam, N., Syfullah, K., & Rahman, R. (2011). [Micro hydro power: promising solution for off-grid](https://www.researchgate.net/profile/Md-Tanbhir-Hoq-2/publication/265010291_Micro_Hydro_Power_Promising_Solution_for_Off-grid_Renewable_Energy_Source/links/5bab044245851574f7e64b63/Micro-Hydro-Power-Promising-Solution-for-Off-grid-Renewable-Energy-Source.pdf) renewable energy source. [International Journal of Scientific &](https://www.researchgate.net/profile/Md-Tanbhir-Hoq-2/publication/265010291_Micro_Hydro_Power_Promising_Solution_for_Off-grid_Renewable_Energy_Source/links/5bab044245851574f7e64b63/Micro-Hydro-Power-Promising-Solution-for-Off-grid-Renewable-Energy-Source.pdf) [Engineering Research,](https://www.researchgate.net/profile/Md-Tanbhir-Hoq-2/publication/265010291_Micro_Hydro_Power_Promising_Solution_for_Off-grid_Renewable_Energy_Source/links/5bab044245851574f7e64b63/Micro-Hydro-Power-Promising-Solution-for-Off-grid-Renewable-Energy-Source.pdf) 2(12), 2-6.

Jeffcoate, P., Whittaker, T., Boake, C., & Elsaesser, B. (2016). Field tests of multiple 1/10 scale tidal turbines in steady flows. *Renewable Energy*, *87*, 240-252. <https://doi.org/10.1016/j.renene.2015.10.004>

Karaalioglu, M. S., & Bal, S. (2022). Performance prediction of cavitating marine current turbine by BEMT based on CFD. *Ocean Engineering*, *255*, 111221. <https://doi.org/10.1016/j.oceaneng.2022.111221>

Khan, M. J., Iqbal, M. T., & Quaicoe, J. E. (2008). River current energy conversion systems: Progress, prospects and challenges.*Renewable and sustainable energy reviews*, *12*(8), 2177-2193. <https://doi.org/10.1016/j.rser.2007.04.016>

Kim, S. J., Singh, P. M., Hyun, B. S., Lee, Y. H., & Choi, Y. D. (2017). A study on the floating bridge type horizontal axis tidal current turbine for energy independent islands in Korea. *Renewable Energy*, *112*, 35-43.

<https://doi.org/10.1016/j.renene.2017.05.025>

Kirke, B. (2020). Hydrokinetic turbines for moderate sized rivers. *Energy for Sustainable Development*, *58*, 182-195. <https://doi.org/10.1016/j.esd.2020.08.003>

Lazzerini, G., Coiro, D. P., Troise, G., & D'Amato, G. (2022). A comparison between experiments and numerical simulations on a scale model of a Horizontal-Axis current turbine. *Renewable Energy*, *190*, 919-934. <https://doi.org/10.1016/j.renene.2022.03.162>

Lee, J. H., Park, S., Kim, D. H., Rhee, S. H., & Kim, M. C. (2012). Computational methods for performance analysis of horizontal axis tidal stream turbines. *Applied energy*, *98*, 512-523. <https://doi.org/10.1016/j.apenergy.2012.04.018>

Lin, Y. T., Chiu, P. H., & Huang, C. C. (2017). An experimental and numerical investigation on the power performance of 150 kW horizontal axis wind turbine. *Renewable Energy*, *113*, 85-93. <https://doi.org/10.1016/j.renene.2017.05.065>

Liu, Q., Miao, W., Ye, Q., & Li, C. (2022). Performance assessment of an innovative Gurney flap for straight-bladed vertical axis wind turbine. *Renewable Energy*, *185*, 1124-1138. <https://doi.org/10.1016/j.renene.2021.12.098>

Lust, E. E., Flack, K. A., & Luznik, L. (2020). Survey of the near wake of an axial-flow hydrokinetic turbine in the presence of waves. *Renewable Energy*, *146*, 2199-2209. <https://doi.org/10.1016/j.renene.2019.08.067>

Mohamed, A. B., Bear, C., Bear, M., & Korobenko, A. (2020). Performance analysis of two vertical-axis hydrokinetic turbines using variational multiscale method. *Computers & Fluids*, *200*, 104432.

<https://doi.org/10.1016/j.compfluid.2020.104432>

Nachtane, M., Tarfaoui, M., Saifaoui, D., & Rouway, M. (2020). Hydrodynamic performance evaluation of a new hydrofoil design for marine current turbines. *Materials Today: Proceedings*, *30*, 889-898.

<https://doi.org/10.1016/j.matpr.2020.04.346>

Nicolli, F., & Vona, F. (2019). Energy market liberalization and renewable energy policies in OECD countries. *Energy Policy*, *128*, 853-867. <https://doi.org/10.1016/j.enpol.2019.01.018>

Nunes, M. M., Junior, A. C. B., & Oliveira, T. F. (2020). Systematic review of diffuser-augmented horizontal-axis turbines. *Renewable and Sustainable Energy Reviews*, *133*, 110075.

<https://doi.org/10.1016/j.rser.2020.110075>

Okulov, V. L., Naumov, I. V., Kabardin, I. K., Litvinov, I. V., Markovich, D. M., Mikkelsen, R. F., ... & Wood, D. H. (2021). Experiments on line arrays of horizontal-axis hydroturbines. *Renewable Energy*, *163*, 15-21. <https://doi.org/10.1016/j.renene.2020.08.148>

Paudel, S., & Saenger, N. (2017). Grid refinement study for three dimensional CFD model involving incompressible free surface flow and rotating object. *Computers & Fluids*, *143*, 134-140. <https://doi.org/10.1016/j.compfluid.2016.10.025>

Puertas-Frías, C. M., Willson, C. S., & García-Salaberri, P. A. (2022). Design and economic analysis of a hydrokinetic turbine for household applications. *Renewable Energy*, *199*, 587-598. <https://doi.org/10.1016/j.renene.2022.08.155>

Pujol, T., Vashisht, A. K., Ricart, J., Culubret, D., & Velayos, J. (2015). Hydraulic efficiency of horizontal waterwheels: Laboratory data and CFD study for upgrading a western Himalayan watermill. *Renewable energy*, *83*, 576-586. <https://doi.org/10.1016/j.renene.2015.04.060>

Roache, P. J. (1994). Perspective: a method for uniform reporting of grid refinement studies. ASME. *J. Fluids Eng. 11*(6), 405-413.

<https://doi.org/10.1115/1.2910291>

Roache, P. J. (1997). [Quantification of uncertainty in](https://www.annualreviews.org/doi/abs/10.1146/annurev.fluid.29.1.123) [computational fluid dynamics.](https://www.annualreviews.org/doi/abs/10.1146/annurev.fluid.29.1.123) Annual review of fluid Mechanics, [29\(1\), 123-160.](https://www.annualreviews.org/doi/abs/10.1146/annurev.fluid.29.1.123)

Roache, P. J. (1998). Verification of codes and calculations. *AIAA journal*, *36*(5), 696-702. <https://doi.org/10.2514/2.457>

Roy, C. J. (2005). Review of code and solution verification procedures for computational simulation. *Journal of Computational Physics*, *205*(1), 131-156. <https://doi.org/10.1016/j.jcp.2004.10.036>

Roy, C. J., & Blottner, F. G. (2006). Review and assessment of turbulence models for hypersonic flows. *Progress in aerospace sciences*, *42*(7-8), 469-530. <https://doi.org/10.1016/j.paerosci.2006.12.002>

Sandoval, J., Soto-Rivas, K., Gotelli, C., & Escauriaza, C. (2021). Modeling the wake dynamics of a marine hydrokinetic turbine using different actuator representations. *Ocean Engineering*, *222*, 108584.

<https://doi.org/10.1016/j.oceaneng.2021.108584>

Shahsavarifard, M., & Bibeau, E. L. (2020). Performance characteristics of shrouded horizontal axis hydrokinetic turbines in yawed conditions. *Ocean Engineering*, *197*, 106916. <https://doi.org/10.1016/j.oceaneng.2020.106916>

Sufian, S. F., Li, M., & O'Connor, B. A. (2017). 3D modelling of impacts from waves on tidal turbine wake characteristics and energy output. *Renewable energy*, *114*, 308-322. <https://doi.org/10.1016/j.renene.2017.04.030>

Tian, W., Mao, Z., & Ding, H. (2018). Design, test and numerical simulation of a low-speed horizontal axis hydrokinetic turbine. *International Journal of Naval Architecture and Ocean Engineering*, *10*(6), 782-793. <https://doi.org/10.1016/j.ijnaoe.2017.10.006>

Wang, W. Q., Yin, R., & Yan, Y. (2019). Design and prediction hydrodynamic performance of horizontal axis microhydrokinetic river turbine. *Renewable energy*, *133*, 91-102. <https://doi.org/10.1016/j.renene.2018.09.106>

Wang, X., Hu, Z. P., Yan, Y., Pei, J., & Wang, W. Q. (2022). Acoustic characteristics of a horizontal axis micro hydrokinetic turbine. *Ocean Engineering*, *259*, 111854. <https://doi.org/10.1016/j.oceaneng.2022.111854>

Wood, D. H., Okulov, V. L., & Vaz, J. R. P. (2021). Calculation of the induced velocities in lifting line analyses of propellers and turbines. *Ocean Engineering*, *235*, 109337. <https://doi.org/10.1016/j.oceaneng.2021.109337>

Woodruff, A. (2007)[. An economic assessment of renewable](http://www.globalislands.net/userfiles/CKIslandspdf2.pdf) [energy options for rural electrification in Pacific Island](http://www.globalislands.net/userfiles/CKIslandspdf2.pdf) [countries. Pacific islands applied geoscience commission](http://www.globalislands.net/userfiles/CKIslandspdf2.pdf) [\(SOPAC\).](http://www.globalislands.net/userfiles/CKIslandspdf2.pdf)

Yang, H., Shen, W., Xu, H., Hong, Z., & Liu, C. (2014). Prediction of the wind turbine performance by using BEM with airfoil data extracted from CFD. *Renewable Energy*, *70*, 107-115. https://doi.org/10.1016/j.renene.2014.05.002

Yuce, M. I., & Muratoglu, A. (2015). Hydrokinetic energy conversion systems: A technology status review. *Renewable and Sustainable Energy Reviews*, *43*, 72-82. <https://doi.org/10.1016/j.rser.2014.10.037>